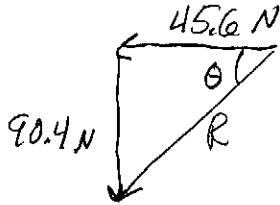


A1)



$$R^2 = (45.6)^2 + (90.4)^2$$

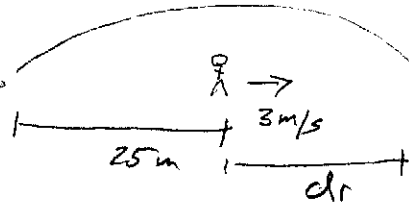
$$R = 101.2 \text{ N}$$

$$\tan \theta = \frac{90.4}{45.6} \quad \theta = 63.2^\circ$$

101 N @ 63.2° S of W

A2) The ball is a projectile and for the receiver to catch it they must be at the same place at the same time.

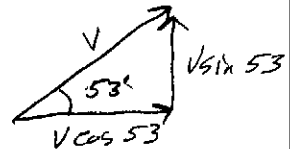
A2)



Receiver

$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$d = 25 + (3)t \quad \text{①}$$



Football

$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$d = v \cos 53 t \quad \text{②}$$

$$0 = v \sin 53 t + \frac{1}{2} (-9.8) t^2$$

$$0 = v \sin 53 - 4.9 t$$

$$t = \frac{v \sin 53}{4.9}$$

① = ②

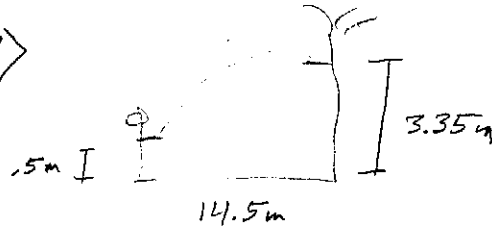
$$25 + 3t = v \cos 53 t$$

$$25 + \frac{3 v \sin 53}{4.9} = v \cos 53 \left[\frac{v \sin 53}{4.9} \right]$$

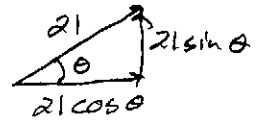
v = 18.6 m/s

A3) The arrow is a projectile,

A3)



$V = 21 \text{ m/s}$



$x) d = d_0 + v_i t + \frac{1}{2} a t^2$

$14.5 = 21 \cos \theta t \rightarrow t = \frac{21 \cos \theta}{14.5}$

$y) d = d_0 + v_i t + \frac{1}{2} a t^2$

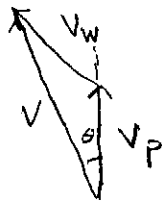
$3.35 = .5 + 21 \sin \theta t + \frac{1}{2} (-9.8) t^2$

$2.85 = 21 \sin \theta \left[\frac{21 \cos \theta}{14.5} \right] - 4.9 \left[\frac{21 \cos \theta}{14.5} \right]^2$

$\theta = 24.2^\circ$

A4) The wind adds to the vel of the plane to come to a final vel.

A4)



$V^2 = V_p^2 + V_w^2 - 2(V_p)(V_w) \cos 135$

$V^2 = (42)^2 + (18)^2 - 2(42)(18) \cos 135$

$V = 56.2 \text{ m/s}$

$\frac{\sin \theta}{V_w} = \frac{\sin 135}{V}$

$\sin \theta = \frac{(18) \sin 135}{56.2 \text{ m/s}}$

$\theta = 13.1^\circ$

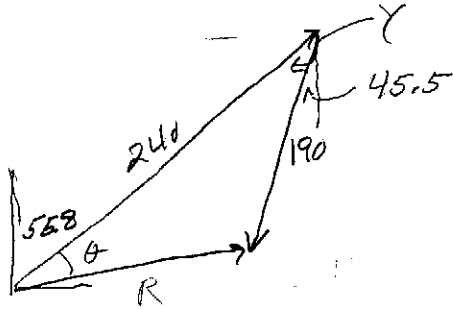
$d = d_0 + v_i t + \frac{1}{2} a t^2$

$d = (56.2)(5)(60)$

$d = 16856 \text{ m}$

$16.8 \text{ km @ } 13.1^\circ \text{ W of N}$

A5 >



$$\gamma = 55.8 - 45.5 = 10.3$$

$$R^2 = (240)^2 + (190)^2 - 2(240)(190) \cos(10.3)$$

$$R = 63.0054$$

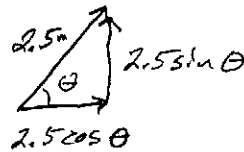
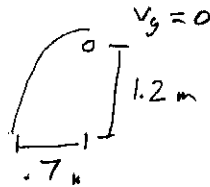
$$\frac{\sin 10.3}{63.0054} = \frac{\sin \theta}{190} \quad \theta = 32.63^\circ$$

$$55.8 + 32.63 = 88.43^\circ$$

63 m/s @ 1.57° N of E

A6 > you are a projectile and hopefully will clear the bar at the top of your path.

A6 >



$$x) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$.7 = 2.5 \cos \theta t \quad t = \frac{.7}{2.5 \cos \theta}$$

$$y) d = d_0 + v_i t + \frac{1}{2} a t^2$$

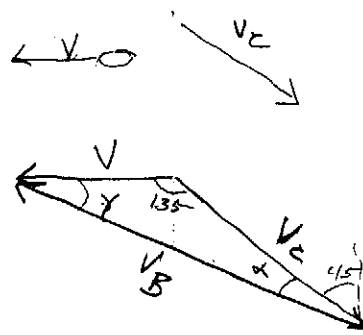
$$1.2 = 2.5 \sin \theta t + \frac{1}{2} (-9.8) t^2$$

$$1.2 = \frac{2.5 \sin \theta (.7)}{2.5 \cos \theta} - 4.9 \left[\frac{.7}{2.5 \cos \theta} \right]^2$$

$$1.2 = .7 \tan \theta - 4.9 \left[\frac{.7}{2.5 \cos \theta} \right]^2$$

$\theta = 42.3^\circ$

A7) The velocity of the boat and velocity of the current will combine vectorially to make a new relative velocity



$$V_B = 12 \text{ m/s}$$

$$V_C = 3.25 \text{ m/s}$$

$$d = 205 \text{ m West}$$

$$\frac{\sin \gamma}{V_C} = \frac{\sin 135^\circ}{V_B}$$

$$\sin \gamma = \frac{(3.25) \sin 135^\circ}{12} \quad \gamma = 11.0408^\circ$$

$$\alpha = 180 - 135 - \gamma \Rightarrow \alpha = 33.96^\circ$$

Steer at 79.0° W of N

$$V^2 = V_B^2 + V_C^2 - 2V_B V_C \cos \alpha$$

$$V^2 = (12)^2 + (3.25)^2 - 2(12)(3.25) \cos (33.96)$$

$$V = 9.47982$$

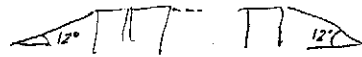
$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$205 = (9.47982) t$$

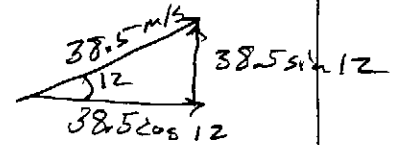
$$t = 21.6 \text{ sec}$$

A8) Sophie is a projectile and thus is controlled by gravity.

A8)



$$L_B = 2.14 \text{ m}$$



$$x) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$n L_B = 38.5 \cos 12 t$$

$$t = \frac{n(2.14)}{38.5 \cos 12}$$

$$y) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$0 = 38.5 \sin 12 t + \frac{1}{2} (-9.8) t^2$$

$$0 = 38.5 \sin 12 - 4.9 t$$

$$0 = 38.5 \sin 12 - 4.9 \left[\frac{2.14 n}{38.5 \cos 12} \right]$$

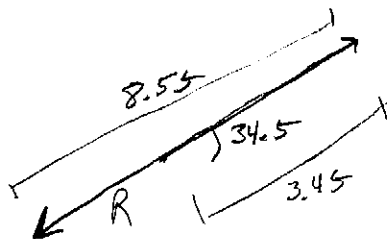
$$4.9 \left[\frac{2.14 n}{38.5 \cos 12} \right] = 38.5 \sin 12$$

$$2.14 n = \frac{(38.5)^2 \sin 12 \cos 12}{4.9}$$

$$n = 28.747$$

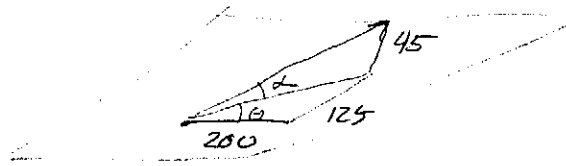
28 busses

B1)



5.10 m/s @ 55.5° S of W

B2> The components of a vector combine to be the vector.



$$d^2 = A^2 + B^2 + C^2$$

$$d^2 = (200)^2 + (125)^2 + (45)^2$$

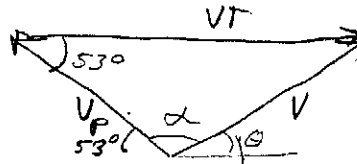
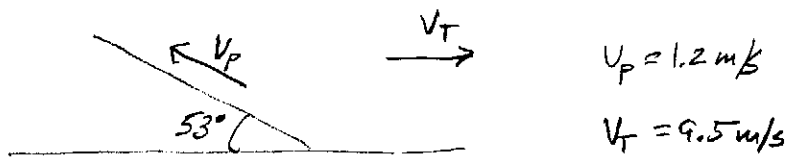
$$d = 240 \text{ m}$$

$$\tan \theta = \frac{125}{200} \quad \theta = 32.0^\circ$$

$$\tan \alpha = \frac{45}{\sqrt{200^2 + 125^2}} \quad \alpha = 10.8^\circ$$

240m @ 32.0° N of E and up 10.8°

B3> The velocities combine to form a new velocity that is with respect to the ground.



$$V^2 = V_p^2 + V_t^2 - 2V_p V_t \cos 53$$

$$V^2 = (1.2)^2 + (9.5)^2 - 2(1.2)(9.5) \cos 53$$

$$V = 8.83 \text{ m/s}$$

$$\frac{\sin \alpha}{V_t} = \frac{\sin 53}{V}$$

$$\sin \alpha = \frac{(9.5) \sin 53}{8.83}$$

$$\alpha = 59.23^\circ$$

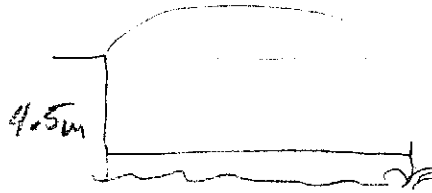
$$180 - 53 - \alpha = \theta$$

$$\theta = 67.8^\circ$$

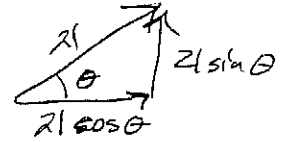
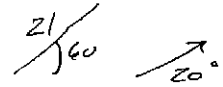
8.83 m/s @ 67.8° up

B4) The cannonball is a projectile. It will have a symmetric around 45° .

B4)



$v = 21 \text{ m/s}$



x) $d = d_0 + v_i t + \frac{1}{2} a t^2$
 $d = 21 \cos \theta t$

y) $d = d_0 + v_i t + \frac{1}{2} a t^2$
 $0 = 4.5 + 21 \sin \theta t + \frac{1}{2} (-9.8) t^2$
 $0 = 4.5 + 21 \sin \theta t - 4.9 t^2$

For $\theta = 20^\circ$

$t = 1.93934 \text{ s}$

$d = 38.3 \text{ m}$

for $\theta = 60^\circ$

$t = 3.944368 \text{ s}$

$d = 41.4 \text{ m}$

for $\theta = 45^\circ$

$t = 3.30807 \text{ s}$

$d = 49.12 \text{ m}$

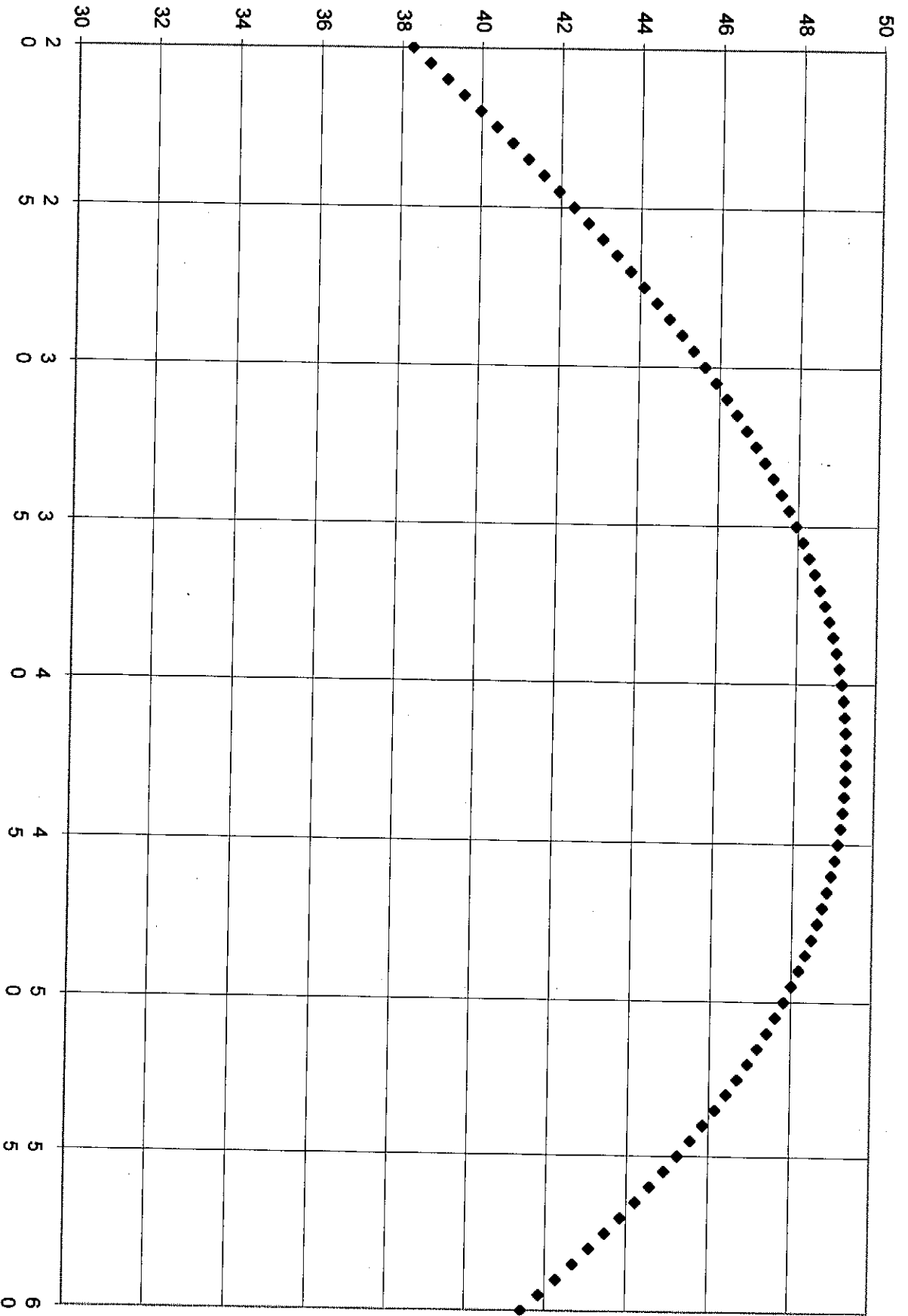
this involve a little calculus.

actually

$\theta = 42.4^\circ$

$t = 3.178774$

$d = 49.3 \text{ m}$



B5 >

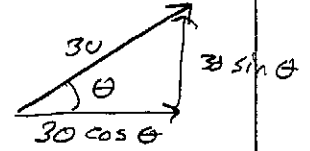
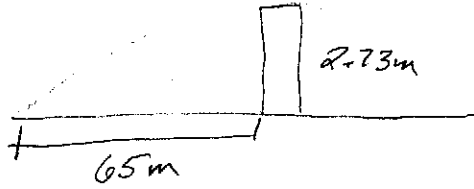
$$34.5\hat{i} + 23\hat{j} + 52.9\hat{k}$$

$$19.4\hat{i} - 27.9\hat{j} + 12.35\hat{k}$$

$$53.9\hat{i} - 4.9\hat{j} + 65.2\hat{k}$$

B6 > The ball is a projectile and must be at the height of the wall when the distance away.

B6 >



$$x) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$65 = 30 \cos \theta t \quad t = \frac{65}{30 \cos \theta}$$

$$y) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$2.73 = 30 \sin \theta t + \frac{1}{2} (-9.8) t^2$$

$$2.73 = 30 \sin \theta t - 4.9 t^2$$

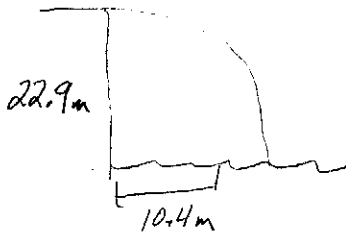
$$2.73 = 30 \sin \theta \left[\frac{65}{30 \cos \theta} \right] - 4.9 \left[\frac{65}{30 \cos \theta} \right]^2$$

$$2.73 = 65 \tan \theta - 4.9 \left[\frac{65}{30 \cos \theta} \right]^2$$

$$\theta = 25.4^\circ$$

B7) The bottle is a projectile it only has a set amount of time to move outward as it falls.

B7)



$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$0 = 22.9 + \frac{1}{2} (-9.8) t^2$$

$$t = 2.162 \text{ s}$$

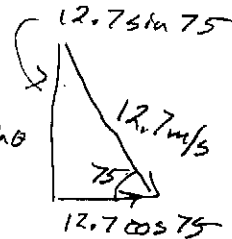
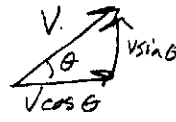
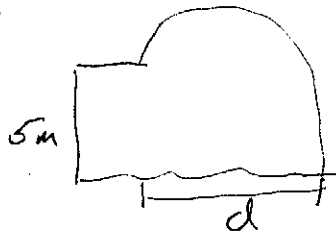
$$x) d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$10.4 = v (2.162)$$

$$v = 4.81 \text{ m/s}$$

B8) The diver is a projectile and so its horizontal vel does not change

B8)



$$V \cos \theta = 12.7 \cos 75 = 3.287$$

$$y) v_f^2 = v_i^2 + 2 a d$$

$$(-12.7 \sin 75)^2 = (V \sin \theta)^2 + 2(-9.81)(-5)$$

$$V \sin \theta = 7.2447$$

$$\frac{V \sin \theta}{V \cos \theta} = \tan \theta = \frac{7.2447}{3.287} \quad \theta = 65.6^\circ$$

$$V \cos 65.6 = 12.7 \cos 75 \quad V = 7.96 \text{ m/s}$$

$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$d = (3.287)(1.991)$$

$$d = 6.54 \text{ m}$$

$$d = d_0 + v_i t + \frac{1}{2} a t^2$$

$$0 = 5 + (7.2447) t + \frac{1}{2} (-9.8) t^2$$

$$t = 1.991 \text{ s}$$